### Carnegie Mellon University Electrical & Computer Engineering

Data-assisted Physics-based Modeling and Simulation for Grid Cybersecurity

AUGUST  $16^{TH}$ , 2022

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## My Journey

### Academic Experience

- Special Faculty at Carnegie Mellon 2020-2022
- Incoming Asst. Professor at the University of Vermont 2023-
- Industry Experience



ISO-NE Summer 2013



Analyzing critical systems in nuclear stations 2012-mid 2015



Commercializing PhD research 2019-2020

### Collaborators



Lujo Bauer



Christos Faloutsos



Bryan Hooi



Shimiao Li



Craig Miller



Larry Pileggi



Vyas Sekar



Brian Singer

# Evolving Grid → Real Cybersecurity Concerns

**Carnegie Mellon University** Electrical & Computer Engineering



• Decarbonization



- Decarbonization
- Electrification



- Decarbonization
- Electrification
- Deteriorating resilience



- Decarbonization
- Electrification
- Deteriorating resilience
- Increasing remote automation

### **Evolving Attack Surface**



## Grid Cybersecurity is a Real Threat Now

### WIRED

### Inside the Cunning, Unprecedented Hack of Ukraine's Power Grid

The hack on Ukraine's power grid was a first-of-its-kind attack that sets an ominous precedent for the security of power grids everywhere.

### Vulnerable U.S. electric grid facing threats from Russia and domestic terrorists



BY BILL WHITAKER FEBRUARY 27, 2022 / 6:57 PM / CBS NEWS

**Carnegie Mellon University** 

### Cyberthreats Discussed in this Talk

- MadIoT threat
- False-data injection attack (FDIA)
- Anomalous Topology Threat



12 Saleh, Prateek Mittal, and H. Vincent Poor. "BlackIoT: IoT botnet of high wattage devices can disrupt the power grid." In 27th {USENIX} Security Symposium ({USENIX} Security 18), pp. 15-32. 2018.

Fig. Ackn. Brian Singer, ECE, CMU Carnegie Mellon University



13 Saleh, Prateek Mittal, and H. Vincent Poor. "BlackIoT: IoT botnet of high wattage devices can disrupt the power grid." In *27th {USENIX} Security Symposium ({USENIX} Security 18)*, pp. 15-32. 2018.

Fig. Ackn. Brian Singer, ECE, CMU Carnegie Mellon University





- False Data Injection Attack (FDIA) spoofs sensor data to cause grid malfunction
  - Key idea: strategically spoof measurement data to bypass existing detection algorithms



16 Liu, Yao, Peng Ning, and Michael K. Reiter. "False data injection attacks against state estimation in electric power grids." ACM Transactions on Information and System Security (TISSEC) 14, no. 1 (2011): 1-33.







## Introduction to Anomalous Topology Threat

- In this threat, an attacker's goal is to change the grid topology
  - E.g., Toggle the circuit breaker for one of two parallel transmission lines



Modeling and Simulation Framework for Cyber-Threat Evaluation

> **Carnegie Mellon University** Electrical & Computer Engineering

### Status Quo in Threat Evaluation - MadIoT

### BlackIoT: IoT Botnet of High Wattage Devices Can Disrupt the Power Grid

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H. Vincent Poor Department of Electrical Engineering Princeton University poor@princeton.edu

### Abstract

We demonstrate that an Internet of Things (IoT) botnet of high wattage devices-such as air conditioners and heaters-gives a unique ability to adversaries to launch large-scale coordinated attacks on the power grid. In particular, we reveal a new class of potential attacks on power grids called the Manipulation of demand via IoT (MadIoT) attacks that can leverage such a botnet in order to manipulate the power demand in the grid. We study five variations of the MadIoT attacks and evaluate their effectiveness via state-of-the-art simulators on real-world power grid models. These simulation results demonstrate that the MadIoT attacks can result in local power outages and in the worst cases, large-scale blackouts. Moreover, wa abow that these attacks are esthan be used to in



### Not Everything is Dark and Gloomy: **Power Grid Protections Against IoT Demand Attacks**

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Alvaro A. Cardenas University of California, Santa Cruz alvaro.cardenas@ucsc.edu

Ross Baldick The University of Texas at Austin baldick@ece.utexas.edu

### Abstract

Devices with high energy consumption such as air conditioners, water heaters, and electric vehicles are increasingly becoming Internet-connected. This new connectivity exposes the control of new electric loads to attackers in what is known as Manipulation of demand via IoT (MadIoT) attacks. In this paper we investigate the impact of MadIoT attacks on power transmission grids. Our analysis leverages a novel cascading outage analysis tool that focuses on how the protection equipment in the power grid as well as how protection algorithms react to cascading events that can lead to a power blackout. In particular, we apply our tool to a large North American regional transmission interconnection system consisting of

work proposed a novel form of attack called Manipulation of demand via IoT (MadIoT) [47], and showed that if an attacker compromised hundreds of thousands of high-energy IoT devices (such as water heaters and air conditioners), the attacker could cause various problems to the power grid, including (i) frequency instabilities, (ii) line failures, and (iii) increased operating costs. These attacks paint a dire picture of the security of the power grid as they show that a 30% increase in demand can trip all the generators in the US Western interconnection causing a complete system blackout, and a 1% increase of demand in the Polish grid results in a cascade of 263 transmission line failures, affecting 86% of the load in the system.

(left) Soltan, Saleh, Prateek Mittal, and H. Vincent Poor. "BlackIoT: IoT botnet of high wattage devices can disrupt the power

grid." In 27th {USENIX} Security Symposium ({USENIX} Security 18), pp. 15-32. 2018.

22 (right) Huang, Bing, Alvaro A. Cardenas, and Ross Baldick. "Not everything is dark and gloomy: Power grid protections against Carnegie Mellon University IoT demand attacks." In 28th {USENIX} Security Symposium ({USENIX} Security 19), pp. 1115-1132. 2019.

### Status Quo in Threat Evaluation - MadIoT

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### Not Everything is Dark and Gloomy: Power Grid Protections Against IoT Demand Attacks

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# Widely varying perceptions on whether comprised IoT devices can cause cascading failure in the electric grid!

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### Status Quo in Threat Evaluation - FDIA



Liu, Yao, Peng Ning, and Michael K. Reiter. "False data injection attacks against state estimation in electric power grids." ACM Transactions on Information and System Security (TISSEC) 14, no. 1 (2011): 1-33. 1. Paraphrased based on discussions with the U.S. grid operators and other researchers in the domain.

- Cyber threats are not studied on realistic grid setups
  - E.g., Did the MadIoT evaluation consider an N-1 secure grid setup?

B. Singer, A. Pandey, S. Li, L. Bauer, C. Miller, L. Pileggi, and V. Sekar, "Shedding light on inconsistencies in grid cybersecurity: Disconnects and recommendations," IEEE Security and Privacy, 2023. (To appear)

25

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26

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- Threat space is not comprehensively explored
  - E.g., Did it consider both hot weather and extreme winter scenarios?
- Simulation tools do not capture the true processes of the grid
  - E.g., Did MadIoT evaluation consider droop, AGC control, and fast reserves?
  - E.g., Did FDIA construction assume ACSE in control rooms?

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27

- Evaluation of cyber threats on unrealistic grid setups
- Threat space is not comprehensively explored
- Simulation tools do not capture the true processes of the grid

Lack of a single universal framework where all grid threats can be analyzed sufficiently accurately!

B. Singer, A. Pandey, S. Li, L. Bauer, C. Miller, L. Pileggi, and V. Sekar, "Shedding light on inconsistencies in grid cybersecurity: Disconnects and recommendations," IEEE Security and Privacy, 2023. (To appear)

## Inspiration from NERC Standards?

• NERC standard TPL-001-4<sup>1</sup> tells system planners how to analyze future systems under a wide range of contingencies:

"Establish Transmission system planning performance requirements within the planning horizon to develop a Bulk Electric System (BES) that will operate reliably over a broad spectrum of System conditions and following a wide range of probable Contingencies."

## Inspiration from NERC Standards?

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• Would a similar methodology help with standardizing the evaluation of cyber threats?

30 1. "NERC Reliability Standards for the Bulk Electric Systems of North America, Standard TPL-001-4 -Transmission System Planning Performance Requirements"

### Threat - Definition

31

### Threat = {Goals, Capabilities} Control 80% Cause of the total cascading IoT devices, grid outage synchronously

B. Singer, A. Pandey, S. Li, L. Bauer, C. Miller, L. Pileggi, and V. Sekar, "Shedding light on inconsistencies in grid cybersecurity: Disconnects and recommendations," IEEE Security and Privacy, 2023. (To appear)

Attack - Definition

### Attack = {Goals, Capabilities, Strategy} Control 80% Crank up the Cause of the total IoT power of all cascading IoT-controlled devices, grid outage synchronously devices

### Attack Scenario - Definition

# Attack Scenario = {Attack, Grid Topology}

Texas grid on a hot summer day!

### A Methodology for Threat Evaluation

Attack Scenarios for Threat



## A Methodology for Threat Evaluation



### A Methodology for Threat Evaluation


### A Methodology for Threat Evaluation



Use a simulator that mimics the real world *sufficiently* well

### A Methodology for Threat Evaluation











### MadIoT Example (cont.)



Generation change in response to increased demand from MadIoT attack
Non-physical simulation because generators exceed their limit
Sum of maximum power output of all generators
Unstable grid region





### FDIA Example



### FDIA Example



### FDIA Example



## FDIA Example (cont.)

- Ran 4 scenarios with varying system knowledge K
  - Key takeaway: the efficacy of the attack is dependent of attacker's knowledge of grid state



47

1 – No attack 2 – FDIA, (ideal) Attacker has perfect system knowledge 3 – FDIA, imperfect topology knowledge  $K_{topo} = 50$ 4 – FDIA, imperfect network parameter knowledge  $K_{\sigma} = 0.02$ 

→  $\tau$  is the critical value of Chi-square distribution → With *RSS* >  $\tau$ , bad-data detection raises an alarm

RSS: Residual sum of squares (also called the J-value)

# DYNWATCH: Physics-driven Data Mining Technique for Anomaly Detection

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### Data Processing in High-voltage Grids



Source: ISO-New England

- Data processing in control rooms
  - AC State-Estimation (ACSE)
  - Topology Estimation (TE)

## Data Processing in High-voltage Grids



Source: ISO-New England

- Data processing in control rooms
  - AC State-Estimation (ACSE)
  - Topology Estimation (TE)
- Fundamental in grid operation

### Data Processing in High-voltage Grids



 Any anomalous data can significantly hamper grid operation

Source: ISO-New England

### Anomalies in ACSE and TE

• Many known causes for anomalies in grid data



• Anomalous data must be identified and isolated for reliable operation

• Setting: spatial features at a single time snapshot



- Setting: spatial features at a single time snapshot
- Measurement data is processed by ACSE and BDD units



- Setting: spatial features at a single time snapshot
- BDD may trigger an anomaly based on the J-value from ACSE



- Setting: spatial features at a single time snapshot
- Some anomalies are not detectable from analysis of spatial patterns alone



- Given sensor data over time, can we detect an anomalous datapoint?
- Time-series processing can detect anomalies that violate temporal statistical consistency (see t = 15)



### Topology Changes → False Positives

Power grid topology changes frequently



### Topology Changes → False Positives

Power grid topology changes frequently





Records from a real utility in the Eastern Interconnection (>17,000 lines)

### Topology Changes → False Positives

- Power grid topology changes frequently
  - Classical approaches can result in false positives (FP)



Interconnection (>17,000 lines)

- The proposed approach on time-series data mining considers the impact of topology change
  - The algorithm has 3 steps



 The proposed approach on time-series data mining considers the impact of topology change



#### 1) Define graph distance

62 S. Li, A. Pandey, B. Hooi, C. Faloutsos and L. Pileggi, "Dynamic Graph-Based Anomaly Detection in the Electrical Grid," in *IEEE Transactions on Power Systems.* 

 The proposed approach on time-series data mining considers the impact of topology change



Define graph distance
 Temporal weighting

63 S. Li, A. Pandey, B. Hooi, C. Faloutsos and L. Pileggi, "Dynamic Graph-Based Anomaly Detection in the Electrical Grid," in *IEEE Transactions on Power Systems.* 

• The proposed approach on time-series data mining considers the impact of topology change



<sup>64</sup> S. Li, A. Pandey, B. Hooi, C. Faloutsos and L. Pileggi, "Dynamic Graph-Based Anomaly Detection in the Electrical Grid," in *IEEE Transactions on Power Systems.* 

### Domain-informed Graph Distance

- The difference between two graphs can be seen as different line outages on the union graph
- Impact of line outage is quantified by line outage distribution factor (LODF)
- Graph distance is the sum of line outage impacts



### Temporal Weighting by Bias-variance Trade-off

- Weigh the past sensor data using a bias-variance trade-off
  - Bias: data from very different topology will increase bias
  - Variance: only using data from the most similar topology will increase variance



### Anomaly Score - Idea

- Learn a distribution of normal behavior while ignoring previous anomalous data
  - Median and IQR are more robust statistics



### Anomaly Score - Construction

• Anomaly score measures the deviation from distribution center

For sensor *s* at time *t*:

$$a_s(t) = \frac{x(t) - \mu(t)}{IQR(t)}$$

Final score for time *t*:

 $A(t) = \max_{s} a_s(t)$ 

 $\mu(t)$  = Weighted Median; IQR(t) = Weighted IQR

### DYNWATCH has Lower False Positives



- False data injection attack (FDIA) is a coordinated attack on grid measurements
- With a constructed FDIA attack, only DYNWATCH is shown to detect all anomalies without False Positives (FP)

## High Performance with Scalability

• DYNWATCH outperforms other classical approaches based on AUC and F-measure





# The proposed method scales (almost) linearly with grid size.

Warm Starter for Cyberthreats-based Contingencies

> **Carnegie Mellon University** Electrical & Computer Engineering

### Intro: Contingency Analysis

- Contingency analysis (CA) is pivotal for grid reliability
  - Evaluates N-1 security: Loss of any 1 device should not cause grid failure
  - Make necessary adjustments if the grid fails N-1 security
## Intro: Contingency Analysis

- Contingency analysis (CA) is pivotal for grid reliability
  - Evaluates N-1 security: Loss of any 1 device should not cause grid failure
  - Make necessary adjustments if the grid fails N-1 security
- CA Requirement: A tool that can solve 10k+ power flow networks within minutes robustly
  - Current tools utilize the pre-contingency solution as the initial condition due to the vicinity to the final solution

## Moving beyond N-1 security for Cyber Resiliency

- Many cyberthreats (MadIoT, substation takeover, etc.) represent N-x events
  - Necessitates that we move beyond N-1 to N-x security
  - Current methods for CA may not work



## Moving beyond N-1 security for Cyber Resiliency

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  - Necessitates that we move beyond N-1 to N-x security
  - Current methods for CA may not work

# CA Requirement for cyberthreats: Robust and fast power flow method for evaluating N-x events

## A Novel Warm Starter Method

- Unlike N-1 contingency evaluation, the N-x contingency solution is not close to the pre-contingency solution
- Tradeoff between robustness and speed
  - Physics-based tools can be made robust but are slow
  - Pure data-driven methods can be fast but may lack robustness

76 Li, Shimiao, Amritanshu Pandey, and Larry Pileggi. "GridWarm: Towards Practical Physics-Informed ML Design and Evaluation for Power Grid." *arXiv preprint arXiv:2205.03673* (2022).

## A Novel Warm Starter Method

- Unlike N-1 contingency evaluation, the N-x contingency solution is not close to the pre-contingency solution
- Tradeoff between robustness and speed
- A warm starter can combine the benefits of both physics-based and data-driven methods

Use ML to learn good initial conditions for N-x events and feed them into the physics-based solver for fast convergence!

<sup>77</sup> Li, Shimiao, Amritanshu Pandey, and Larry Pileggi. "GridWarm: Towards Practical Physics-Informed ML Design and Evaluation for Power Grid." *arXiv preprint arXiv:2205.03673* (2022).

## Graph-based Warm Starter Model

- Power grid is an interconnected graph
  - Voltages at a node are a function of neighboring node voltages



Contingency information

<sup>78</sup> Li, Shimiao, Amritanshu Pandey, and Larry Pileggi. "GridWarm: Towards Practical Physics-Informed ML Design and Evaluation for Power Grid." *arXiv preprint arXiv:2205.03673* (2022).

## Graph-based Warm Starter Model

- Power grid is an interconnected graph
- The joint distribution of postcontingency voltages conditioned on contingency & system information can be described via a pairwise Markov Random Field (cMRF) model:

$$P(y|x,\theta) = \frac{1}{Z(\theta,x)} \prod_{i=1}^{n} \psi_i(y_i) \prod_{(s,t)\in E}^{n} \psi_i(y_s,y_t)$$



Contingency information

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#### Conditional Gaussian Random Field (cGRF) Model

• Assume the cMRF model to be Gaussian (cGRF)

$$P(y|x,\theta) = \frac{1}{Z(\theta,x)} \prod_{i=1}^{n} \psi_i(y_i) \prod_{(s,t)\in E}^{n} \psi_i(y_s,y_t)$$
  
if  $P(y|x,\theta)$  is Gaussian then:  
$$\psi_i(y_i) = exp\left(-\frac{1}{2}y_i^T \Lambda_i y_i + \eta_i^T y_i\right)$$
  
$$\psi_i(y_s,y_t) = exp(-\frac{1}{2}y_s^T \Lambda_{st} y_t)$$

## Conditional Gaussian Random Field (cGRF) Model

- Assume the cMRF model to be Gaussian (cGRF)
  - Use local neural nets to model parameters in  $\Lambda$  and  $\eta$
  - Apply domain knowledge to choose the feature space

$$P(y|x,\theta) = \frac{1}{Z(\theta,x)} \prod_{i=1}^{n} \psi_i(y_i) \prod_{(s,t)\in E}^{n} \psi_i(y_s,y_t)$$
  
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$$A = \begin{bmatrix} \Lambda_1 & \frac{1}{2}\Lambda_{(1,2)} & 0 & \frac{1}{2}\Lambda_{(1,4)} \\ \frac{1}{2}\Lambda_{(1,2)}^T & \Lambda_2 & \frac{1}{2}\Lambda_{2,3} & \frac{1}{2}\Lambda_{2,4} \\ \frac{1}{2}\Lambda_{(1,4)}^T & \frac{1}{2}\Lambda_{(2,4)}^T & \frac{1}{2}\Lambda_{(3,4)}^T & \Lambda_4 \end{bmatrix}, \eta = \begin{bmatrix} \eta_1 \\ \eta_2 \\ \eta_3 \\ \eta_4 \end{bmatrix}$$

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$$M_i = \left[ \begin{array}{c} \Lambda_1 & \frac{1}{2}\Lambda_{(1,2)} & 0 & \frac{1}{2}\Lambda_{(1,4)} \\ \frac{1}{2}\Lambda_{(1,2)}^T & \Lambda_2 & \frac{1}{2}\Lambda_{(2,4)} \\ \frac{1}{2}\Lambda_{(2,4)}^T & \frac{1}{2}\Lambda_{(2,4)} \\ \frac{1}{2}\Lambda_{(2,4)}^T & \frac{1}{2}\Lambda_{(3,4)} \\ \frac{1}{2}\Lambda_{(3,4)}^T & \frac{1}{2}\Lambda_{(3,4)} \\$$

## cGRF Model Inference

• With a trained model parameters  $\hat{\theta}_x = [\hat{\theta}_{\Lambda}, \hat{\theta}_{\eta}]$ , given  $x_{test}$ ,  $\hat{y}_{test}$  can be inferred:

$$\widehat{\Lambda} = f_{\Lambda}(x_{test}, \widehat{\theta}_{\Lambda})$$
$$\widehat{\eta} = f_{\eta}(x_{test}, \widehat{\theta}_{\eta})$$
$$\widehat{\Lambda} \, \widehat{y}_{test} = \widehat{\eta}$$

## Physical Interpretability

- The proposed warm starter provides a linear proxy for grid operation post-contingency
- The linear proxy  $(\Lambda, \eta)$  is structurally similar to post-contingency admittance matrix at solution  $Y_{bus}$ , J



## Including Domain Knowledge

• Developed three variants of graphical model-based warm starter: cGRF, cGRF-PS, cGRF-ZI

Domain Knowledge	cGRF	cGRF-PS	cGRF-ZI
Graphical Nature of the Grid	Y	Y	Υ
Parameter Sharing	N	Y	Y
Zero Injection Nodes	Ν	Ν	Y

## Results: Proposed Warm starter (cGRF)



On average, we observe a 5x speed improvement over traditional initialization methods

(b) 2000-bus case.

# Conclusions

- Research goal: Develop analytical tools for grid cybersecurity
  - Special focus on combining data-driven and physics-based techniques
- Very interested in collaborations to maximize the impact